

People's Democratic Republic of Algeria
Ministry of Higher Education and Scientific research
M'hamed Bougara University, Boumerdes
Institute of Electrical and Electronic Engineering,
Laboratory of Signals and Systems (LSS)



ALGERIAN JOURNAL OF SIGNALS AND SYSTEMS

ISSN : 2543-3792

Title: Fault Detection in Wide Area Monitoring Systems via PMU Optimal Placement

Authors: Abdelmadjid RECIOUI, Mohamed TAZIBT and Hakim BENCHENI

Affiliations:

Signals and Systems Laboratory, IGEE, UMBB University, 35000; Boumerdes, Algeria,

Page range: 149- 161

IMPORTANT NOTICE

This article is a publication of the Algerian journal of Signals and Systems and is protected by the copyright agreement signed by the authors prior to its publication. This copy is sent to the author for non-commercial research and education use, including for instruction at the author's institution, sharing with colleagues and providing to institution administration. Other uses, namely reproduction and distribution, selling copies, or posting to personal, institutional or third party websites are not allowed.

Volume : 2 Issue : 3 (September 2017)

Laboratory of Signals and Systems

Address : IGEE (Ex-INELEC), Boumerdes University, Avenue de l'indépendance, 35000, Boumerdes, Algeria

Phone/Fax : 024 79 57 66

Email : lss@univ-boumerdes.dz ; ajsyssig@gmail.com

©LSS/2017

Fault Detection in Wide Area Monitoring Systems via PMU Optimal Placement

Abdelmadjid RECIOUI, Mohamed TAZIBT and Hakim BENHENNI

Laboratory of Signals and Systems, Institute of electrical and electronic engineering, University M'hamed Bougara of Boumerdes, Avenue de l'indépendance, 35000, Boumerdes, Algeria.
a_recioui@univ-boumerdes.dz

Abstract: The Phasor measurement units (PMUs) have become more and more attractive in power engineering as they can provide synchronized measurements of real-time voltage and currents phasors. The objective of this work is twofold: first, the optimal placement of PMUs is done in the standardized IEEE systems. Next, fault location is determined based on the measurements collected from these PMUs. The simulations are carried out using MATLAB SIMULINK. The results show that it is possible to exploit the PMU measurement data to locate and hence cure the faults in the power system.

Keywords: Smart grids, Phasor measurement units, PMU placement, fault location.

1. INTRODUCTION

Wide Area Measurement System (WAMS) based on synchronized phasor measurement technology has been gaining increasingly interests due to its great value in power system dynamic monitoring, potential applications in system modeling and validation and system wide protection and control [1]. Phasor Measurement units (PMUs) can offer accurate node voltage and current phasors referring to the same time-space coordinate. They can enhance many applications such as state estimation and bad data detection [2], stability control [3], remedial action schemes [4], and disturbance monitoring [5]. As the voltage and current phasors are measured, the equations of state estimation problem become linear and the solution can be obtained straightforwardly [6].

It is neither reasonable nor practical to install a PMU at each bus of a wide-area power network. As a result, the problem of optimal PMU placement (OPP) concerns where and how many PMUs should be implemented to a power system to achieve full observability at minimum number of PMUs [7-9]. Using the data provided by PMUs installed in some appropriate bus nodes of a power network, one can construct a new type of measuring system to improve the observability and the precision of the power system state estimator. The observability depends on the type, the number and the geographic distribution of measurements [10].

Several works have been done to efficiently place phasor measurement units (PMUs) in terms of both measurement accuracy and cost effectiveness. The problem has been addressed in [11-13]. Phadke *et al.* [11] explored the possibility of providing all the nodes of the system with PMU's for state estimation purpose. The problem which has been defined in [13] is to determine the placement of the minimal set of PMU's which makes the system observable. Attention has been also drawn to the use of evolutionary heuristic algorithms in optimal PMU placement. In [14] a modified bisecting search and simulated annealing method based on topological observability have been used. In [15], a genetic algorithm is used to find the optimal PMU locations. In [16] and [17], the authors use integer programming to find the minimum number and locations of PMUs. In [18] and [19] the authors propose an exhaustive search based methodology to determine the minimum number and optimal locations of PMUs for complete observability of the power system. The particle swarm optimization (PSO) technique has been used successfully in a number of power system applications [20-21].

In this work, interest goes to the implementation through simulation of the results already obtained in previous works [8-9]. The complete system is implemented with the PMUs placed at their optimal locations. The measurement data obtained through simulation are compared to the healthy case to find where the fault has occurred and to correct this fault so that it does not propagate in the remaining parts of the system.

2. PMU OPTIMAL PLACEMENT

2.1. PMU placement for state estimation

The PMUs receive signals from GPS satellites and provide synchronized measurements from different locations to the desired destination known as the phasor data concentrator (PDC) [22]. In this work, the PDC is represented as the graphical user interface GUI. The measurement data can be used for wide area monitoring; real time dynamics and stability monitoring; dynamic system ratings, and improvements in state estimation, protection, and control [23].

When a PMU is placed at a bus, it can measure the voltage phasor at that bus, as well as at the buses at the other end of all the incident lines, using the current phasor and the known line parameters. It is assumed that the PMU has a sufficient number of channels to measure the current phasors through all the branches incident to the corresponding bus. It is to be noted here that the errors in the voltage and current measurements by the PMU and the transmission line parameters induce uncertainties in the estimated voltage phasor at the other end of the line [23].

The current measurement capability of PMUs was examined so as to estimate the voltage phasors at some buses by using Kirchhoff's current law (KCL) (when applicable) [24]. In the case of a power injection measurement at a bus, if the voltage phasors of all but one connected bus are known, the remaining one can be estimated by using KCL. However, it is clear that the measurement errors propagate further due to the use of KCL. In this chapter, the use of current measurements by the PMUs to estimate voltage phasors is therefore proposed to be limited only to the relative buses [23].

The location of the PMUs makes the system observable as a normal operating condition, as well as for the outage of a single transmission line. A topological observability analysis is carried out to identify the unobservable branch flows in the system. The terminal buses of the branches with unobservable flows are taken as the candidate locations for placing the PMUs [25].

2.2. System description

The idea of using phasor measurements unit for system monitoring applications is not new. Earlier work done introduces the use of PMUs for such applications. This work is later extended to the investigation of optimal location of PMUs where each PMU is assumed to provide voltage and current phasors at its associated bus and all incident branches. It is therefore possible to fully monitor the system by using relatively small number of PMUs much less than the number of buses in the system. The whole process starts with the sensors that are connected to the indicated busses (2, 6 and 9) and (3, 5, 10, 12, 18, 23, 27) for 14 bus and 30 bus systems respectively. That optimal placement for the PMUs was treated using non-linear constraints [22]. Then depending on the type of PMUs which provide two types of measurements: bus voltage phasors and branch current phasors; in this report .A dedicated low-latency PDC has been presented as a Graphical User Interface [26].

2.3. Bus systems

Two standardized IEEE bus systems are considered: the 14 and 30 bus systems. For the 14-bus system, PMUs are installed in network system to measure the voltage and current samples from various location points. For IEEE 14 bus, previous work found that one needs to place the PMUs in 2-6-9, respectively [22]. As PMUs are interlinked to Global positioning system, samples from both PMUs and GPS are analyzed using MATLAB/ SIMULINK [27].

Validation of results of the 14 bus system

As it has been found in past works [8-9], there must be three PMUs to be placed at buses 2, 6 and 9, respectively. Bus 7 is the only zero injection bus. The PMU at bus 2 can not only measure the voltage of bus 2, but also the current of branches 2-1, 2-3, 2-4 and 2-5. Using Ohm's law, the voltage at buses 1, 3, 4 and 5 can be obtained from the branch currents and the voltage at bus 2. Having determined voltage at buses 1, 2, 3, 4, and 5, the current of branches 1-5, 3-4 and 4-5 can be calculated.

By following the same logic, PMU at bus 6 can measure the voltage at bus 6 and the current of branches 6-5, 6-11, 6-12 and 6-13, thus allowing the calculation of the voltage at buses 5, 11, 12, 13 and the current of branch 12-13.

PMU at bus 9 can measure the voltage at bus 9 and the current of branches 9-4, 9-7, 9-10, 9-14 and allow the calculation of the voltage at buses 4, 7, 10, 14, and the current of branches 4-7. As

voltage of buses 10, 11, 13, 14 are known, current of branches 10-11 and 13-14 can now also be calculated.

Using the known current of branches 4-7 and 9-7, and the zero injection at bus 7, the current of branch 7-8 can be derived using the Kirchhoff's Current Law. The only remaining unknown voltage at bus 8 can now be calculated by using the voltage at bus 7 and the current of branch 7-8. Thus the entire system becomes observable by placing only three PMUs at buses 2, 6, 9 and by considering the zero injection at bus 7.

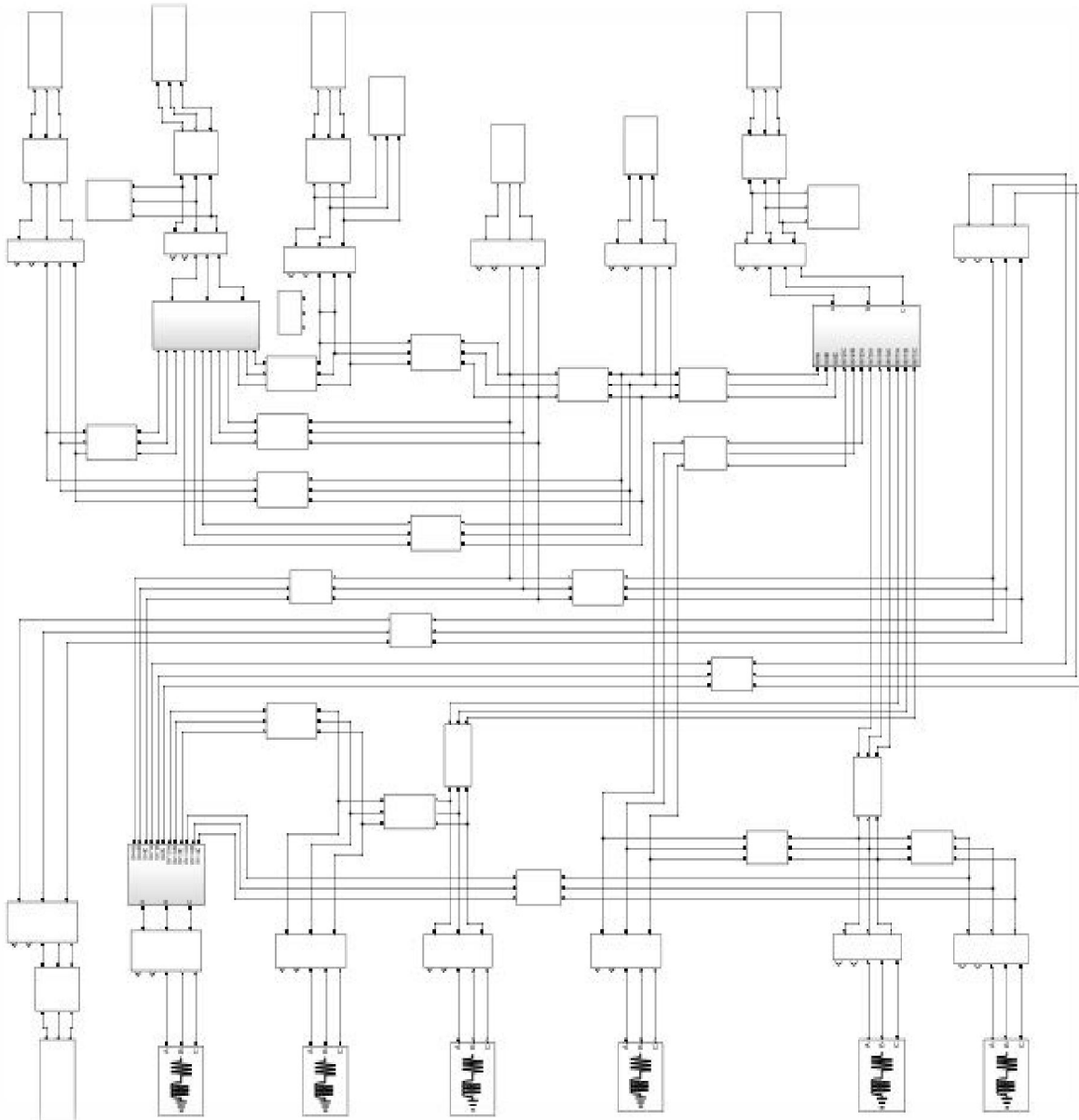


Fig. 1 IEEE 14 buses with PMUs

The PMUs collect phasors data from busses 2,6 and 9 then sends to the PDC. The simulation of the system show results as it must be represented in PDC (GUI in our case) Figure 2 represents a control center as a GUI; it was designed by a MATLAB script language. This shows the results of the measurements in the IEEE 14 bus network; where PMUs collect phasor data of indicated busses.

The ability of PMU is to measure the voltage phasor of a bus at which it is placed and the current phasors of all lines connected to that bus. It means PMU can make the installed bus and its neighbouring buses observable. The values at others buses are calculated by applying KCL.

Figure 3 shows the variation of the Voltage V with respect to time for all 14 nodes. We can see that the system is healthy and stable and we can deduct from its stability that no fault is occurring in the system. The values are in a range between 0.4 pu and 1.8 pu.

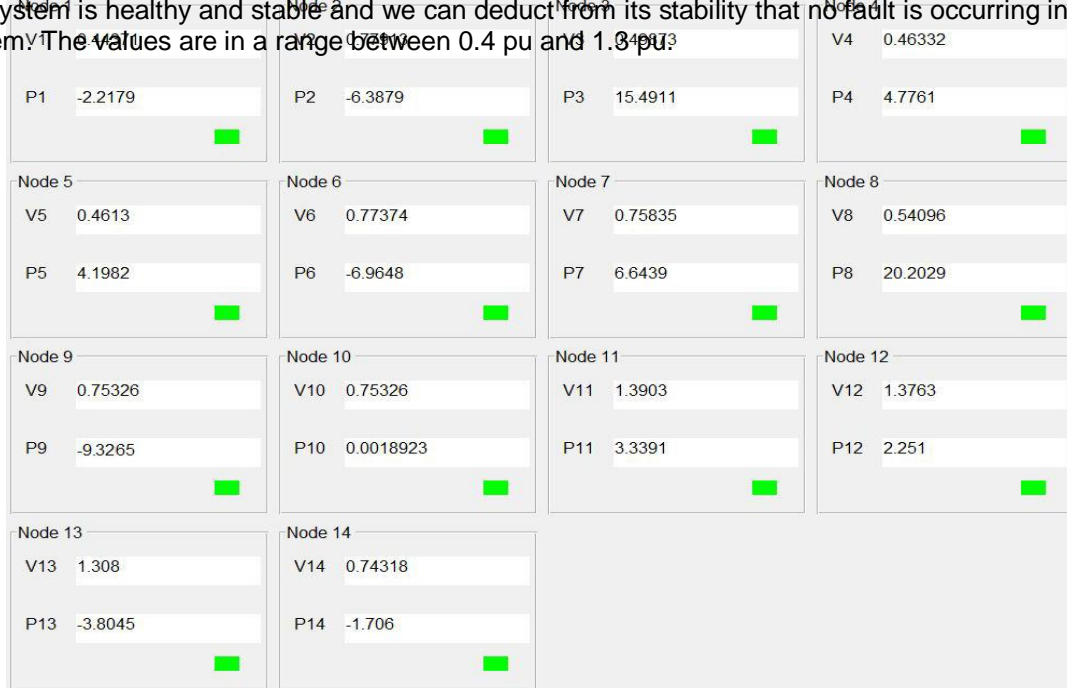


Fig. 2. The graphical user interface for IEEE 14 buses

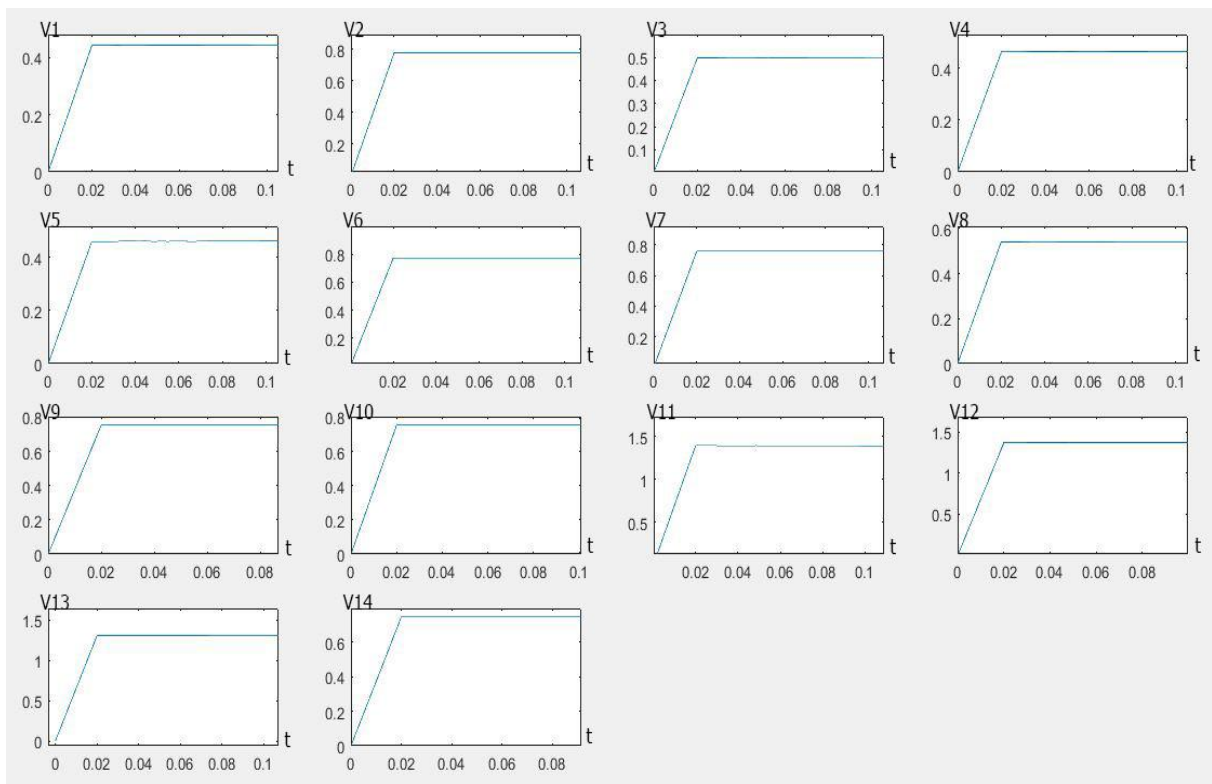


Fig. 3 The corresponding voltages (voltage in PU versus time in 1 second) for IEEE 14 buses respectively.

For the IEEE 30-bus system, a similar work is done as for the 14-bus system in MATLAB/SIMULINK as shown in fig. 4. Taking into consideration a system with zero injections and

the Non-linear constraints algorithm to determine the optimal placement, PMUs are placed in the 3, 5, 10, 12, 18, 23 and 27 in IEEE 30 buses [8-9].

Analysis and results of the system

There are seven PMUs placed at buses 3, 5, 10, 12, 18, 23 and 27. Bus 6, 9, 11, 25, 28 are the zero injection buses [22]. The PMU at bus 3 can not only measure the voltage of bus 3 but also the current of branches 3-1, 3-4. Using Ohm's law, the voltage at buses 1 and 4 can be obtained from the branch currents and the voltage at bus 3. Having determined voltage at buses 1, 3 and 4, the current of branches 1-2 and 2-4 can be calculated. By following the same logic steps for the PMUs at 10, 12, 18, 23 and 27. Thus the entire system becomes observable by placing only seven PMUs. A MATLAB script is written to display bus voltages in per units and angles in degrees as shown in fig. 5.

Figure 6 shows the variation of the Voltage V with respect to time for all 30 nodes. The PDC represented in GUI makes the state of the system network observable. The voltage magnitude and phase angle at each bus is displayed with stable values. The evaluated system is said to be healthy.

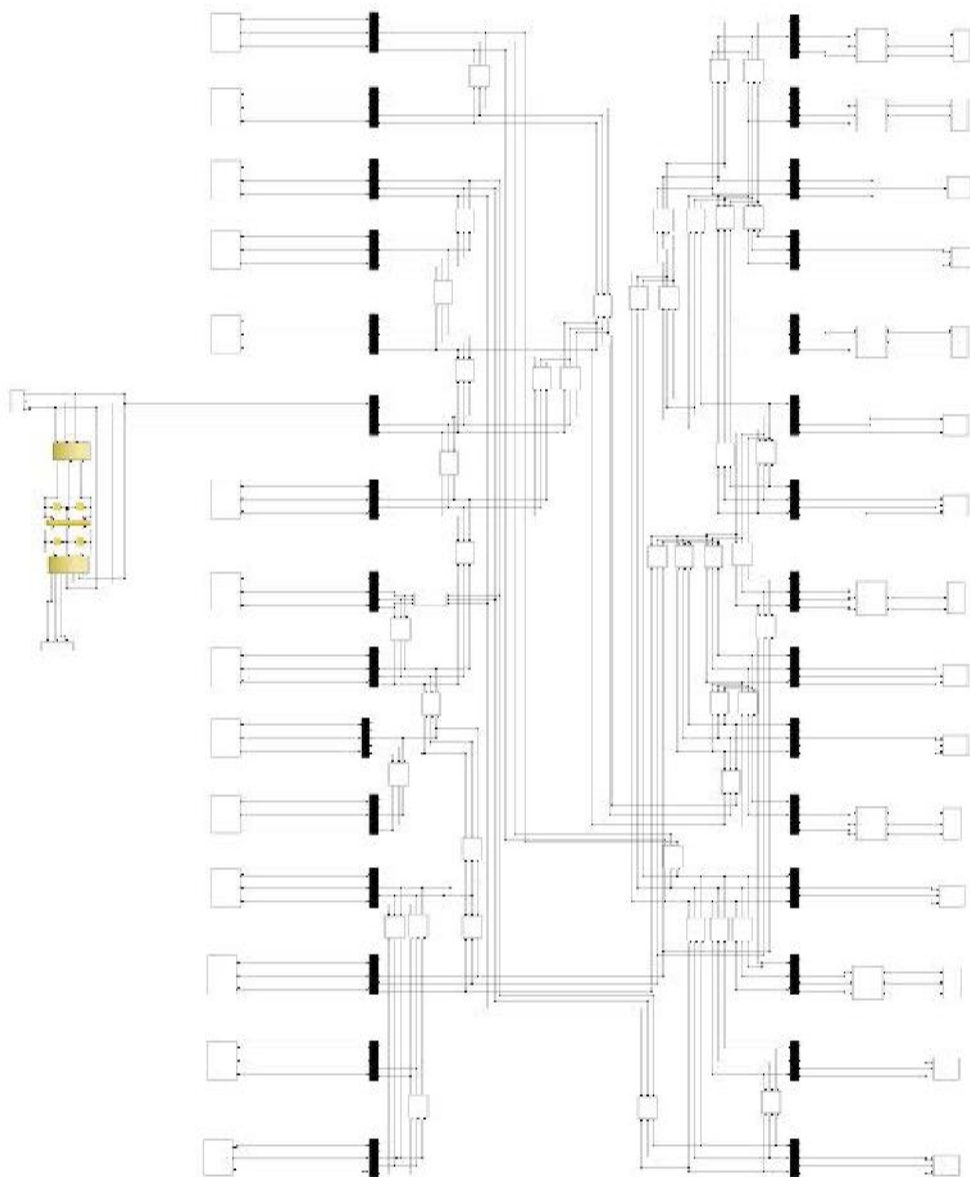


Fig. 4 IEEE 30-bus system Simulink model

Node 1 V1 0.401930 P1 79.0219	Node 2 V2 0.42830 P2 2.1721	Node 3 V3 0.7245 P3 -67.2835	Node 4 V4 0.6513 P4 13.5881	Node 5 V5 0.4362 P5 -146.9622	Node 6 V6 0.3369 P6 -85.5057
Node 7 V7 0.62719 P7 14.8989	Node 8 V8 0.43004 P8 17.5008	Node 9 V9 0.550215 P9 -87.2143	Node 10 V10 0.6392 P10 -134.248	Node 11 V11 0.54048 P11 -88.8894	Node 12 V12 0.6735 P12 -52.3129
Node 13 V13 0.44684 P13 87.2717	Node 14 V14 0.35662 P14 31.7988	Node 15 V15 0.40364 P15 38.4236	Node 16 V16 0.4701 P16 30.9556	Node 17 V17 1.0533 P17 -76.6247	Node 18 V18 0.4344 P18 -107.9559
Node 19 V19 0.7297 P19 29.043	Node 20 V20 1.09265 P20 -53.0744	Node 21 V21 0.6009 P21 43.6554	Node 22 V22 0.351605 P22 -71.6575	Node 23 V23 0.70318 P23 -149.7874	Node 24 V24 0.4377 P24 31.6511
Node 25 V25 1.2018 P25 57.9145	Node 26 V26 0.35696 P26 53.2287	Node 27 V27 1.0704 P27 -147.7104	Node 28 V28 0.67645 P28 -89.9098	Node 29 V29 0.70406 P29 67.2086	Node 30 V30 0.37394 P30 54.7237

Fig. 5 The graphical user interface for IEEE 30-bus system

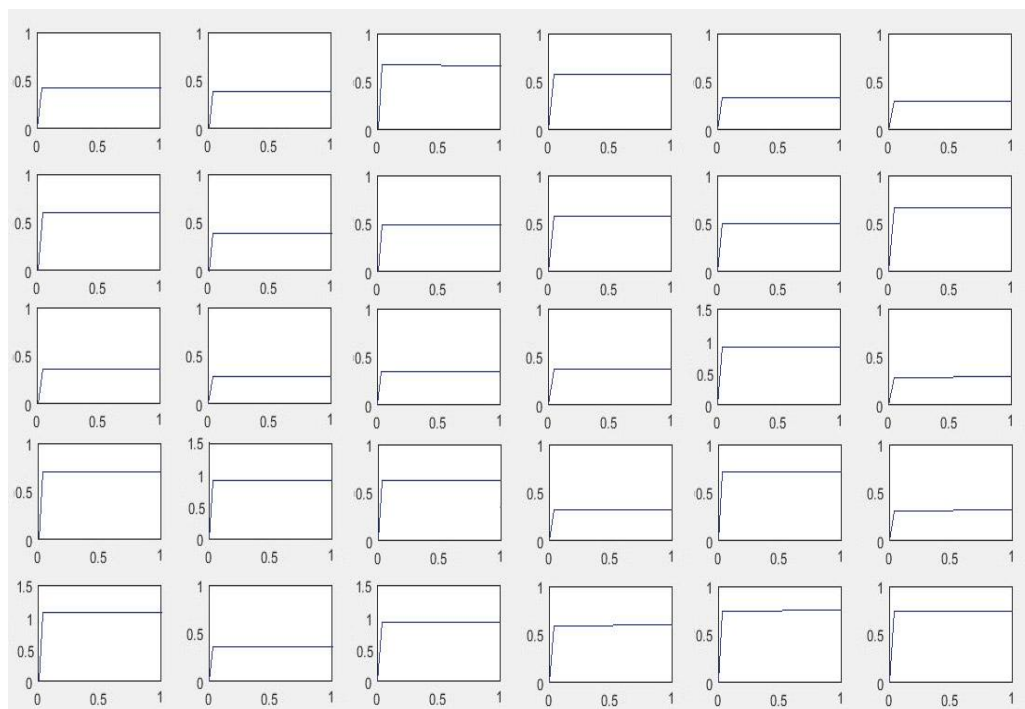


Fig. 6 The corresponding voltages (voltage in PU versus time in 1 second) for IEEE 30 buses respectively

3. FAULT DETECTION USING PMUs

In this section, different types of faults are to be induced each time in different location placement. The synchronized fault voltages are monitored by neighboring PMUs installed at indicated busses. These detects the measurements abnormalities either a voltage drop in bus or a current spike between two busses. Based on the calculated fault node injection, fault nodes can be deduced or fault locations in transmission lines can be calculated.

3.1. Faults in IEEE 14 bus system

Fault in a bus carrying a PMU

A line to ground fault is placed in bus 2; a bus carrying PMU.

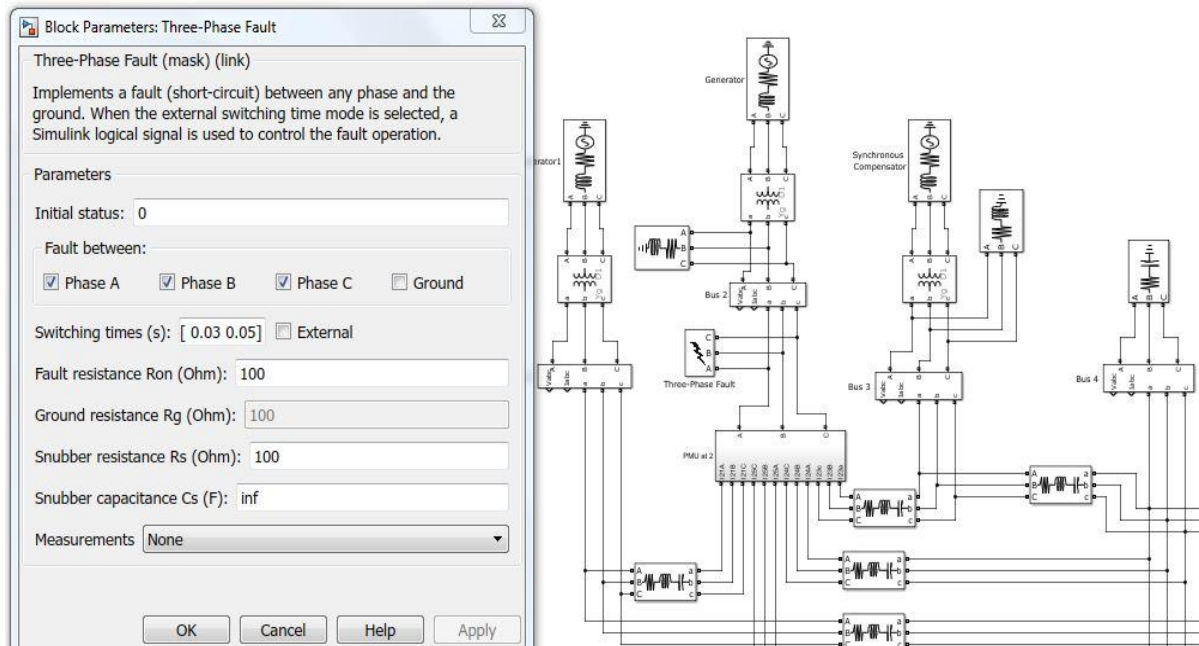


Fig. 7 Simulink model for a fault in bus 2

By creating a three phase balanced fault in bus 2 the PDC (GUI in our case) displays what is presented in the fig. 8.

Node 1 V1 0.31352 P1 -4.0495	Node 2 V2 0.67881 P2 -6.4283	Node 3 V3 0.38816 P3 23.3164	Node 4 V4 0.33666 P4 7.2386
Node 5 V5 0.33075 P5 5.0247	Node 6 V6 0.7735 P6 -6.9872	Node 7 V7 0.75845 P7 6.8864	Node 8 V8 0.44533 P8 26.0661
Node 9 V9 0.75298 P9 -9.2265	Node 10 V10 0.75135 P10 -0.33282	Node 11 V11 1.454 P11 3.2011	Node 12 V12 1.4402 P12 2.1748
Node 13 V13 1.3716 P13 -3.6282	Node 14 V14 0.74041 P14 -2.1561		

Fig. 8 IEEE 14 buses fault detected on bus 2 in interface

The program written in MATLAB script reacts when difference in voltages occurs for healthy system and unhealthy system, then it detects the fault in the defected bus 2.

Fig. 9 is a graph representation of the fault happening during time period [0.3; 0.5] in bus 2, the changes of voltages are remarkable comparing with the GUI in chapter 3. During this fault the graph of voltages V in each bus is changed because of the current spike. Voltage changes occur in the all interconnected busses.

According to the graph the voltages decreases when the fault occurs, the changes happened in bus 2 (the faulty bus) and the buses interconnected with it, bus 1,3,4,5 and 8. We can see that the system is unhealthy and unstable and we can deduce that the system is faulty. So, the system will be unstable.

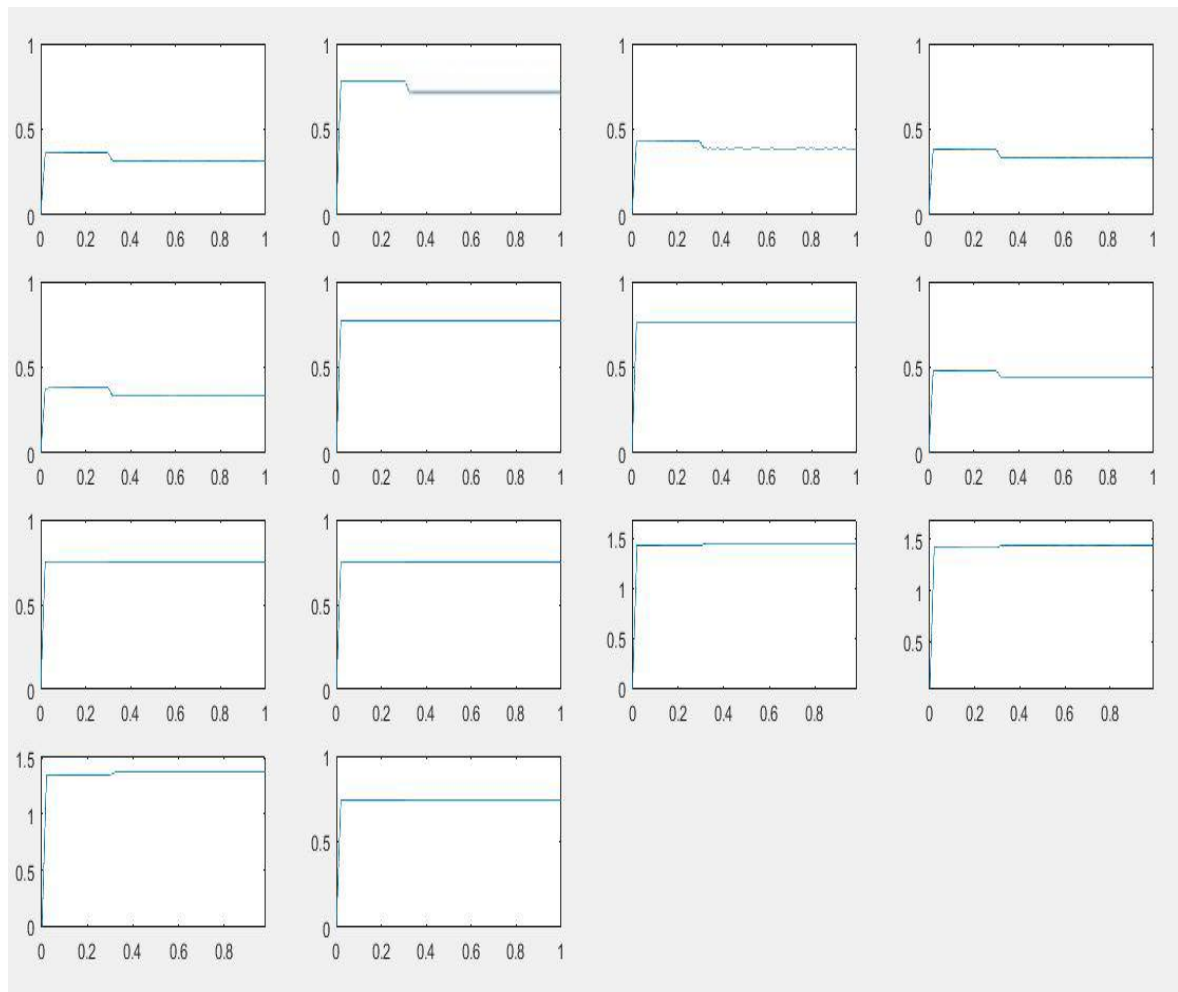


Fig. 9 voltage graph (voltage in PU versus time in 1 second) IEEE 14 buses respectively

Fault in a bus without PMU

Now a line to ground fault is induced in the transmission line between bus 11 and bus 12, those two busses do not carry PMU. By creating a line to ground fault between bus 11 and bus 12, the results are displayed in the figure 10.

Even there is no PMU placed in buses 11 and 12, the fault is detected in GUI due to the collected data from the related PMU, so the optimal placement of PMU makes the whole system observable and the fault is detectable.

Figure 11 shows the change of voltage that occurs when this type of fault happens, the graph points that the interconnected busses are affected by the fault happened in the transmission line between bus 11 and bus 12.

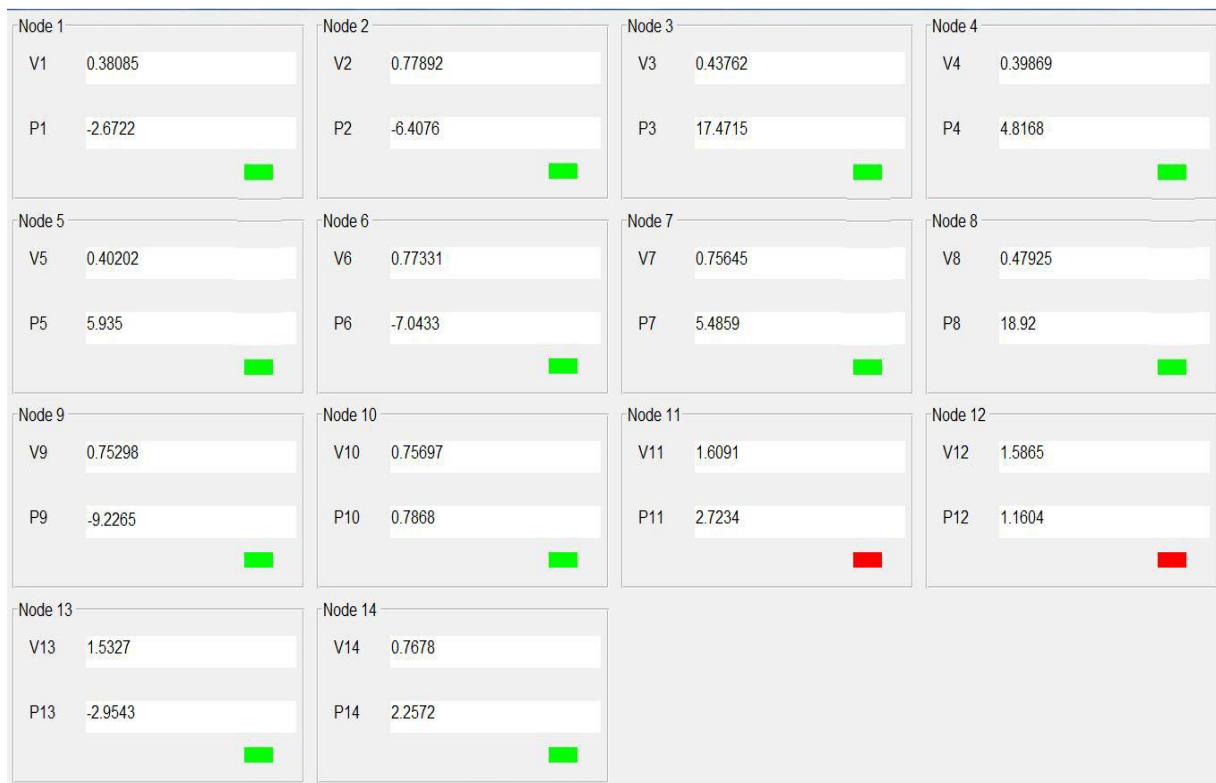


Fig. 10 Voltage (in PU) versus time in 1 second- IEEE 14 buses fault detected between buses 11 and 12

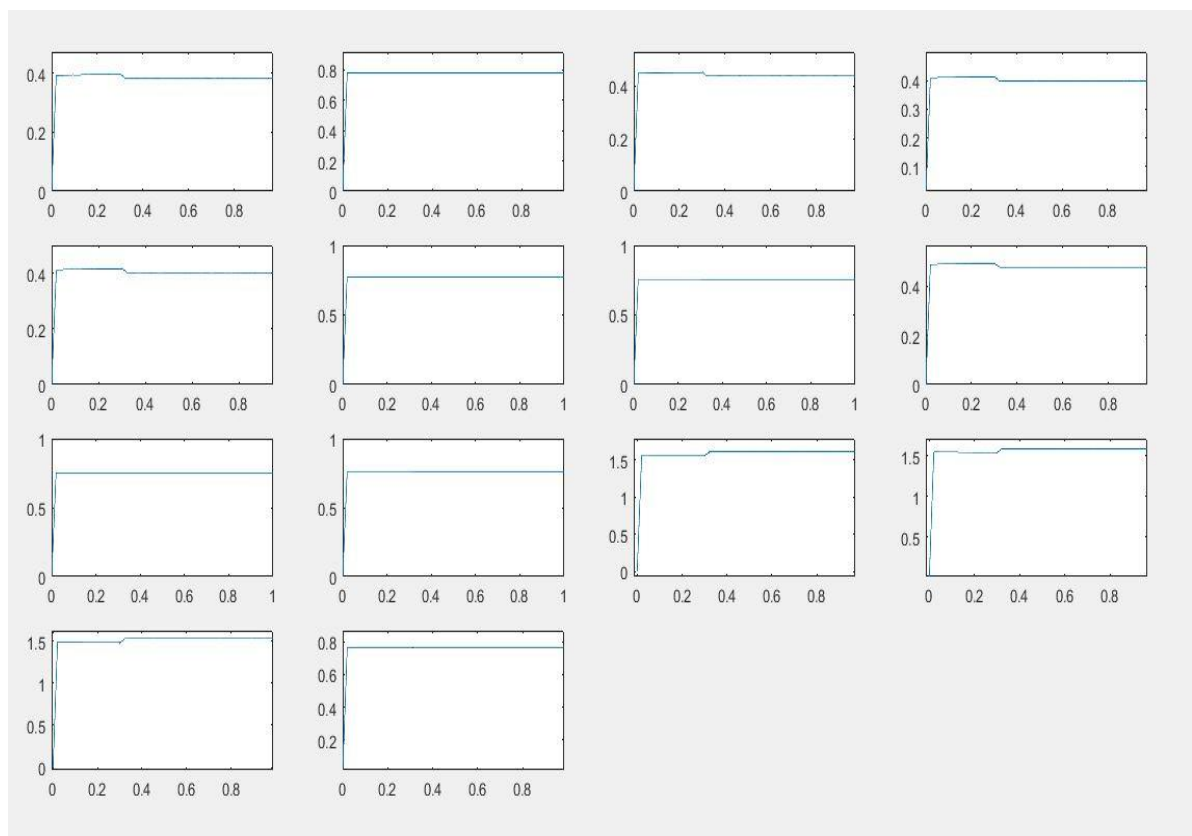


Fig. 11 Voltage (in PU) versus time in 1 second- IEEE 14 bus system

3.2. Faults in IEEE 30-bus system

Fault in a bus carrying PMU

We applied The same work that we have done for IEEE 14 buses in IEEE 30 buses , first the fault locates in bus 3 the bus carried PMU.

The PMU detects the fault and indicates in Graphical User Interface which is used as a control center to facilitate the observability of the system for the workers as shown in Figure 12.

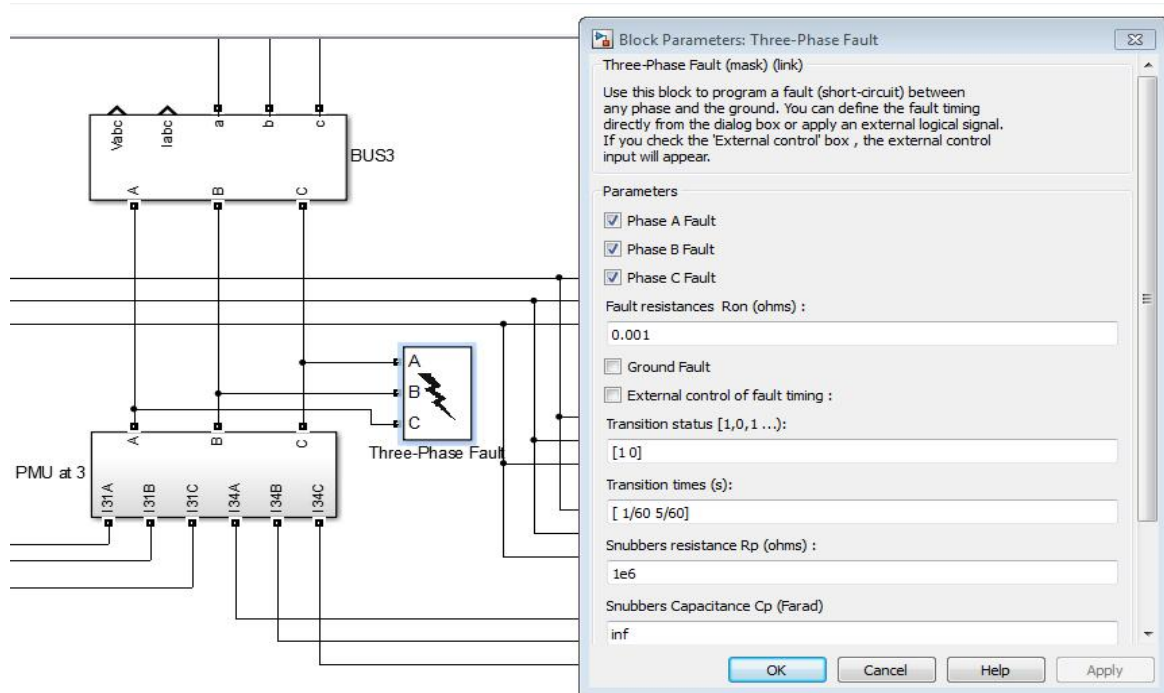


Fig. 12 Simulink model for a fault in bus 3

Node 1 V1 0.401930 P1 79.9479	Node 2 V2 0.42830 P2 2.7314	Node 3 V3 0.6445 P3 -57.0845	Node 4 V4 0.52406 P4 16.5881	Node 5 V5 0.4362 P5 -146.9402	Node 6 V6 0.3369 P6 -84.1297
Node 7 V7 0.62719 P7 19.9889	Node 8 V8 0.43004 P8 17.5008	Node 9 V9 0.550215 P9 -87.2143	Node 10 V10 0.6392 P10 -135.048	Node 11 V11 0.54048 P11 -88.8504	Node 12 V12 0.6735 P12 -52.4349
Node 13 V13 0.44684 P13 88.0817	Node 14 V14 0.35662 P14 31.7988	Node 15 V15 0.40364 P15 36.0336	Node 16 V16 0.4701 P16 31.9215	Node 17 V17 1.0533 P17 -76.4347	Node 18 V18 0.4344 P18 -124.5359
Node 19 V19 0.7297 P19 29.883	Node 20 V20 1.09265 P20 -53.2714	Node 21 V21 0.6009 P21 43.6554	Node 22 V22 0.351605 P22 -72.3375	Node 23 V23 0.70318 P23 -137.7314	Node 24 V24 0.4377 P24 31.0311
Node 25 V25 1.2018 P25 58.1435	Node 26 V26 0.35696 P26 53.6057	Node 27 V27 1.0704 P27 -147.7104	Node 28 V28 0.67645 P28 -89.7018	Node 29 V29 0.70406 P29 67.3496	Node 30 V30 0.7394 P30 54.3947

Fig. 13 IEEE 30-bus system fault detected for bus 3 in interface.

There is a decrease of voltages in the nodes interconnected with the faulty bus (three balanced fault).

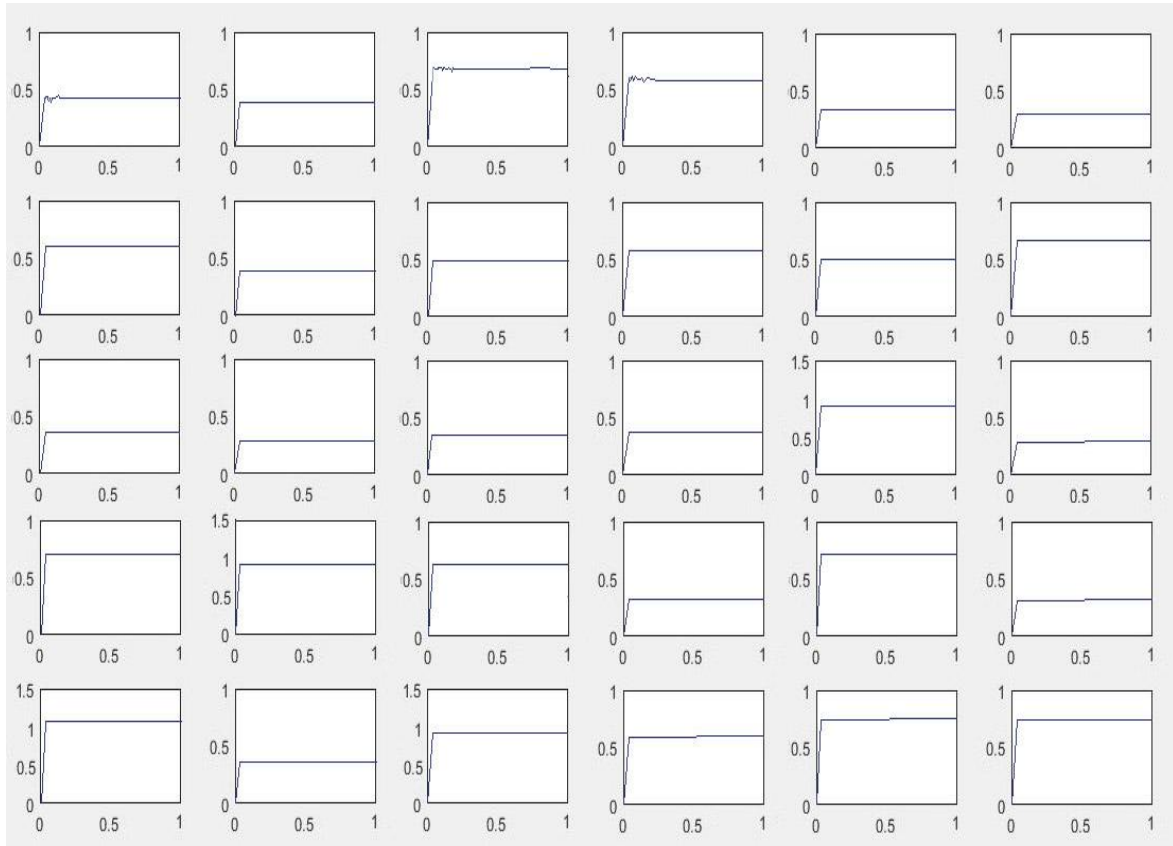


Fig. 14 (voltage in PU versus time in 1 second) IEEE 30 buses respectively

Fault in a bus without PMU

The fault is created between buses 22 and 24 in Simulink.

Node 1 V1 0.401930 P1 79.1719	Node 2 V2 0.42830 P2 2.2821	Node 3 V3 0.7245 P3 -67.5835	Node 4 V4 0.00016951 P4 13.6081	Node 5 V5 0.0011783 P5 -146.8822	Node 6 V6 0.3369 P6 -85.3157
Node 7 V7 0.62719 P7 14.8989	Node 8 V8 0.43004 P8 17.5008	Node 9 V9 0.550215 P9 -87.2143	Node 10 V10 0.5192 P10 -134.605	Node 11 V11 0.54048 P11 -88.7494	Node 12 V12 0.6735 P12 -52.5429
Node 13 V13 0.44684 P13 87.2717	Node 14 V14 0.35662 P14 31.7988	Node 15 V15 0.40364 P15 38.4236	Node 16 V16 0.4701 P16 30.9556	Node 17 V17 1.0533 P17 -76.6247	Node 18 V18 0.4344 P18 -107.9559
Node 19 V19 0.7297 P19 29.043	Node 20 V20 1.09265 P20 -53.0744	Node 21 V21 0.4309 P21 43.2374	Node 22 V22 0.471605 P22 -71.9571	Node 23 V23 0.53318 P23 -149.6274	Node 24 V24 0.5477 P24 31.3511
Node 25 V25 1.3518 P25 57.2655	Node 26 V26 0.35696 P26 53.3887	Node 27 V27 1.0704 P27 -147.7104	Node 28 V28 0.67645 P28 -89.9098	Node 29 V29 0.70406 P29 67.2086	Node 30 V30 0.7394 P30 54.7237

Fig. 15 IEEE 30 buses fault detected between buses 22 and 24 in interface

The figure below shows the variation of the Voltage V with respect to time for all 30 nodes. We can see that the system is unhealthy and unstable and we can deduce from that that a fault is occurring in the system. So, the system will be unstable. There are also changes in voltages.

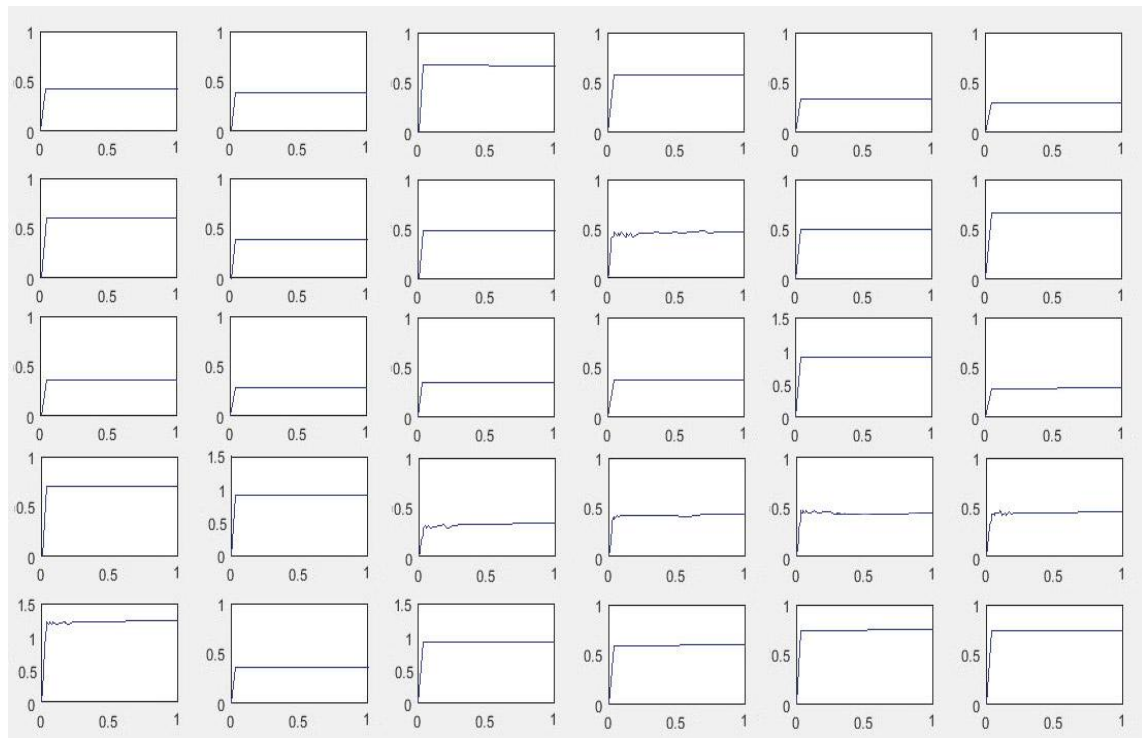


Fig. 16 Voltage (in PU) versus time in 1 second for IEEE 30 buses

CONCLUSION

In this work, the use of PMUs to detect and locate faults in a power system has been investigated. The purpose is to locate and isolate the faulty part of the system so that to prevent the propagation of the fault to the remaining parts of the power system and find a solution to the problem. The idea was to compare the measurement data using the PMUs under the faulty conditions to those recorded for the healthy system. The technique adopted here resembles the neural network training and the simulation results have shown the successfulness of the adopted approach.

An extension of the work would be to use renewable energy sources to correct the detected faults and heal the system and restore it to its healthy state. A final product would be a self healing system that automatically detects, locates and corrects the fault.

References

- [1] Matthew C. Valenti, and Ali Feliachi (2002), Communication Delays in Wide Area Measurement Systems ,BijuNaduvathuparambil, Dept. of Comp. Sci. & Elect. Eng. West Virginia University Morgantown, IEEE.
- [2] Waheed Ur Rahman, Muhammad Ali, AmjadUllah, Hafeez Ur Rahman, MajidIqbal, Haseeb Ahmad, Adnan Zeb, Zeeshan Ali, M. Ahsan Shahzad, Beenish (2012), Advancement in Wide Area Monitoring Protection and Control Using PMU's Model in MATLAB/SIMULINK Taj, Smart Grid and Renewable Energy, (3): 294-307.
- [3] Barley C. D. and Winn C. B. (1996), Optimal dispatch strategy in remote hybrid power systems, solar energy; 58(4-6):165-79
- [4] Barley C. D. , Winn C. B., Flowers L. and Green H. J. (1995), Optimal control of remote hybrid power systems. Part I. Simplified model. In: Proceedings of Wind Power 95.
- [5] Christian Sasse et al., Office for Official Publications of the European Communities (2006), European Smart grids technology platform,
- [6] Xu B. and Abur A. (2005). Optimal placement of phasor measurement units for state estimation, Final Project Report, PSERC.
- [7] Xu B. (2006),optimal monitoring and visualization of steady state power system operation, Ph.D Dissertation, Texas A&M University.

-
- [8] Abdelmadjid Recioui, "Application of the Teaching Learning based Optimization to the optimal placement of phasor measurement units", book chapter in handbook of emergent applications of optimization algorithms, IGI global, 2017.
- [9] Recioui A., Bentarzi H., Ouadi A. (2015) Application of a Binary Teaching Learning-Based Algorithm to the Optimal Placement of Phasor Measurement Units. In: Dincer I., Colpan C., Kizilkan O., Ezan M. (eds) Progress in Clean Energy, Volume 1. Springer, Cham
- [10] Xu Bei, Yeo Jun Yoon and Ali Abur (2008), Optimal placement and utilization of phasor measurements for state estimation, Texas A&M University.
- [11] T. L. Baldwin, L. Mili, M. B. Boisen and R. Adapa (1993), Power System Observability with Minimal Phasor Measurement Placement, IEEE Transactions on Power Systems, 8(2):707-715.
- [12] Arun G. Phadke., James S. Thorp (2008), Synchronized Phasor Measurements and Their Applications, Blacksburg, Virginia.
- [13] Phadke A. G. (1993), Synchronized phasor measurements in power systems, IEEE Computer Applications in Power, 6(2):10-15.
- [14] Nuqui R. F. and Phadke A. G. (2005), Phasor Measurement Unit placement techniques for complete and incomplete observability, IEEE Trans. Power Delivery, 20(4): 2381-2388.
- [15] Milosevic B. and Begovic M. (2003), Nondominated sorting genetic algorithm for optimal phasor measurement placement," IEEE Trans. Power Syst., 18(1):69-75.
- [16] Xu B. and Abur A. (2004). Observability analysis and measurement placement for systems with PMUs, in proc. IEEE Power Eng. Soc. Power Systems Conf. Expo.: 943-946.
- [17] B. mohammadi-lvatloo (2009), Optimal placement of PMUs for power system observability using topology based formulated algorithms, Sahrf University of technology P. O. Box 11365-8639. Tahrn.Iran.
- [18] Chakrabarti S. and Kyriakides E. (2007). Optimal placement of phasor measurement units for state estimation, in Proc. 7th IASTED Int. Conf. Power and Energy Systems, Palma de Mallorca, Spain:1-6.
- [19] Chakrabarti S. and Kyriakides E. (2008). Optimal placement of phasor measurement units for power system observability, IEEE Trans. Power Syst.,23(3):1433-1440.
- [20] Hajian M., A. , Ranjbar M., Amraee T., and Shirani A. R. (2007). Optimal Placement of Phasor Measurement Units: Particle Swarm Optimization Approach, in proc. Of the 14th International Conference on Intelligent System Applications to Power Systems, ISAP 2007, Kaohsiung, Taiwan.
- [21] Sharma Charu and Tyagi Barjeev. (2011), An approach for optimal PMU placement using binary particle swarm optimization with conventional measurements, International Journal of Engineering, Science and Technology, 3(3): 56-63.
- [22] James Momoh, (2012) SMART GRID: Fundamentals of Design and Analysis, WILEY & SONS.
- [23] Mohammad-Reza MOSAVI, Amir-Ali AKHYANI, Abdolreza RAHMATI (2012),"A PMU Placement Optimal Method in Power Systems using Modified ACO Algorithm and GPS Timing, Iran University of Science and Technology.
- [24] Sanjay Damhare, Devesh Dua, Rajeev Kumar Gajbhiye, S. A. Soman (2008), Optimal Zero: An ILP Approach, Indian Institute of Technology, July 14-18.
- [25] Mohammad Shahraeini, M. Hossein Javidi (2011), A Survey on Topological Observability of Power Systems, IEEE.
- [26] jiangnon.P.,S., yuanzhang, and H,F wang, "Optimal Placement for full Network Observability using Tabu Search Algorithm", int .J.Elect. Power energy syst., 23; 1525-1526.
- [27] Ganga Reddy Tankasala, Sridhar Sanisetty, Varun Kumar Vala (2012), □Optimal Placement of Phasor Measurement Units for State Estimation using Artificial Intelligence Techniques□.International Journal of Scientific & Engineering Research 3(2).